

The astrophysics of black hole mergers

1. Pairing massive BHs in galactic nuclei
from large to small scales, role of gas
 2. Electromagnetic signatures of massive BH binaries
in EM observations or in GW detections
 3. Where do massive BHs come from anyway?
protogalaxy formation after the cosmic dark age
 - ~~4. [Stellar-mass BH binaries]
in AGN accretion disks with EM signatures~~
-

Where Do Massive BHs Come From?

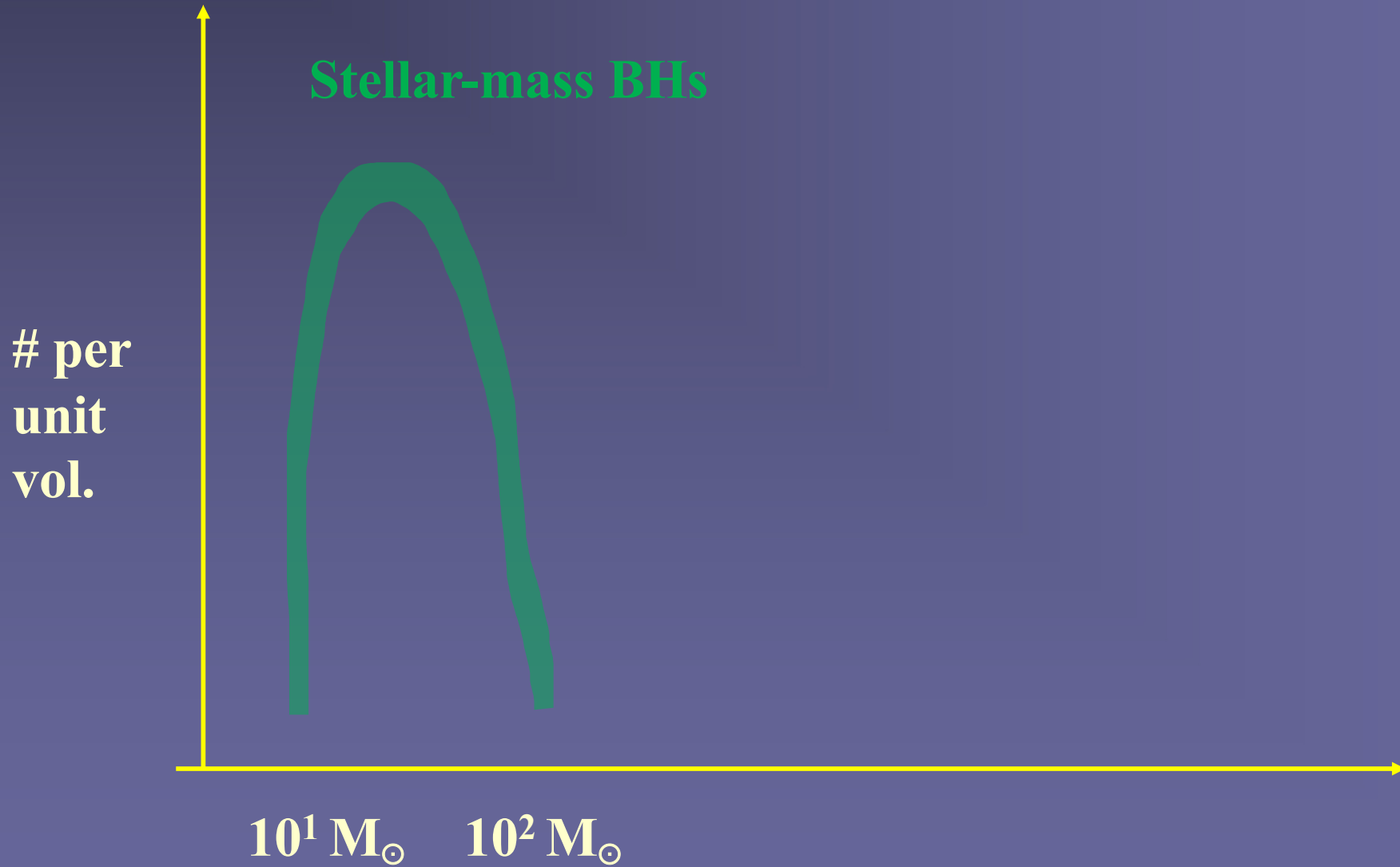
Zoltán Haiman
Columbia University

Lecture 3

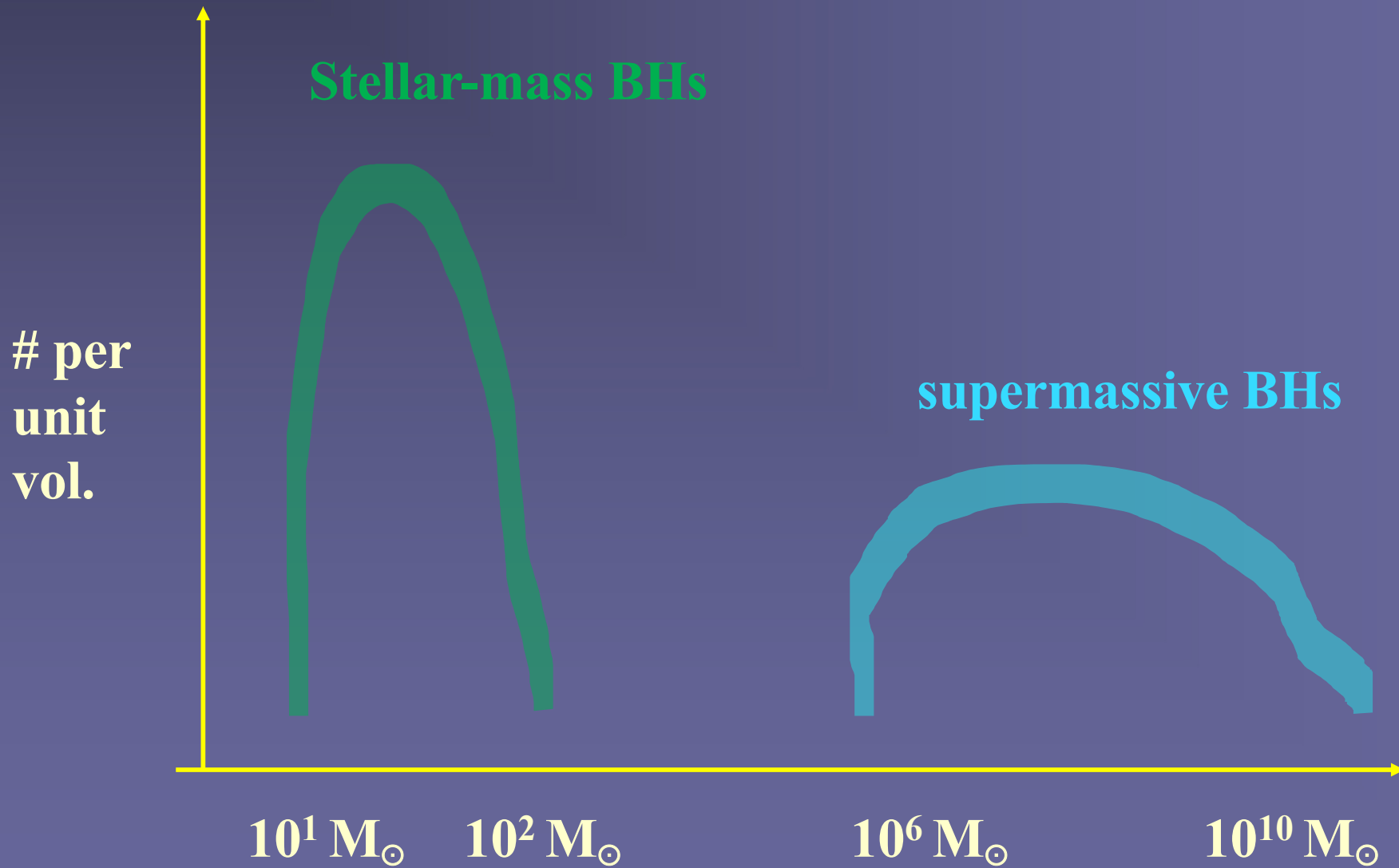
Outline

1. **Observations: types of black holes in the universe**
 2. **Theory: where do massive black holes come from?**
 3. **The Future: how to distinguish different pathways?**
-

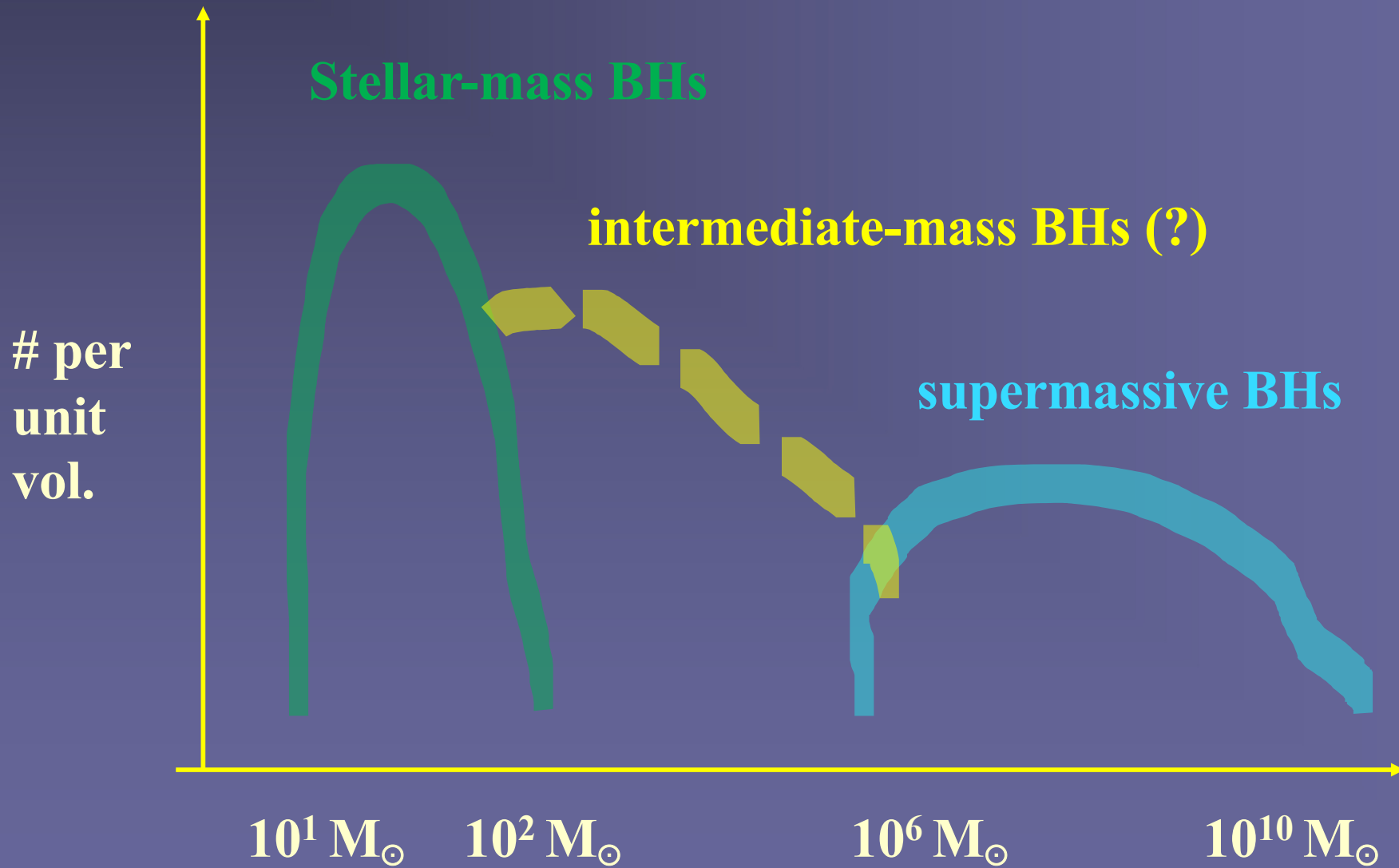
Black Hole Population



Black Hole Population



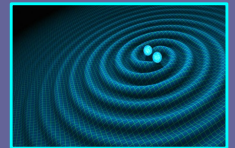
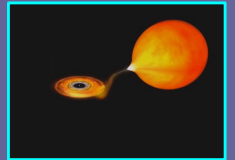
Black Hole Population



Two types of black holes

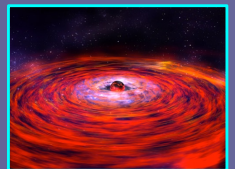
- Stellar-mass BHs:

- End fate of massive stars – well understood
- Birth masses limited to $\text{few } M_{\odot} \lesssim M \lesssim 60 M_{\odot}$
- 100 million in a typical galaxy like the Milky Way (0.1% of stars)
- detected only when they have a partner: *X-ray binary* or *GWs*
- can be seen only in nearby universe (dozens) – too faint otherwise



- (Super-) massive BHs:

- One (or a few?) in center of each galaxy, $M_{\text{BH}} = \text{few} \times 10^{-4} M_{\text{stars}}$
- Masses limited to $10^6 M_{\odot} \lesssim M \lesssim 10^{10} M_{\odot}$
- 100 detected indirectly (*gas/stars speeds* $\sim 0.1c$) or imaged (*M87, SgrA**)
- 1% are “active”, visible to the edge of the universe as quasars (~ 1 million)
- origin unknown, but likely formed early on



- Intermediate-mass BHs (?):

- probably not in large numbers, but difficult to detect

Quasars

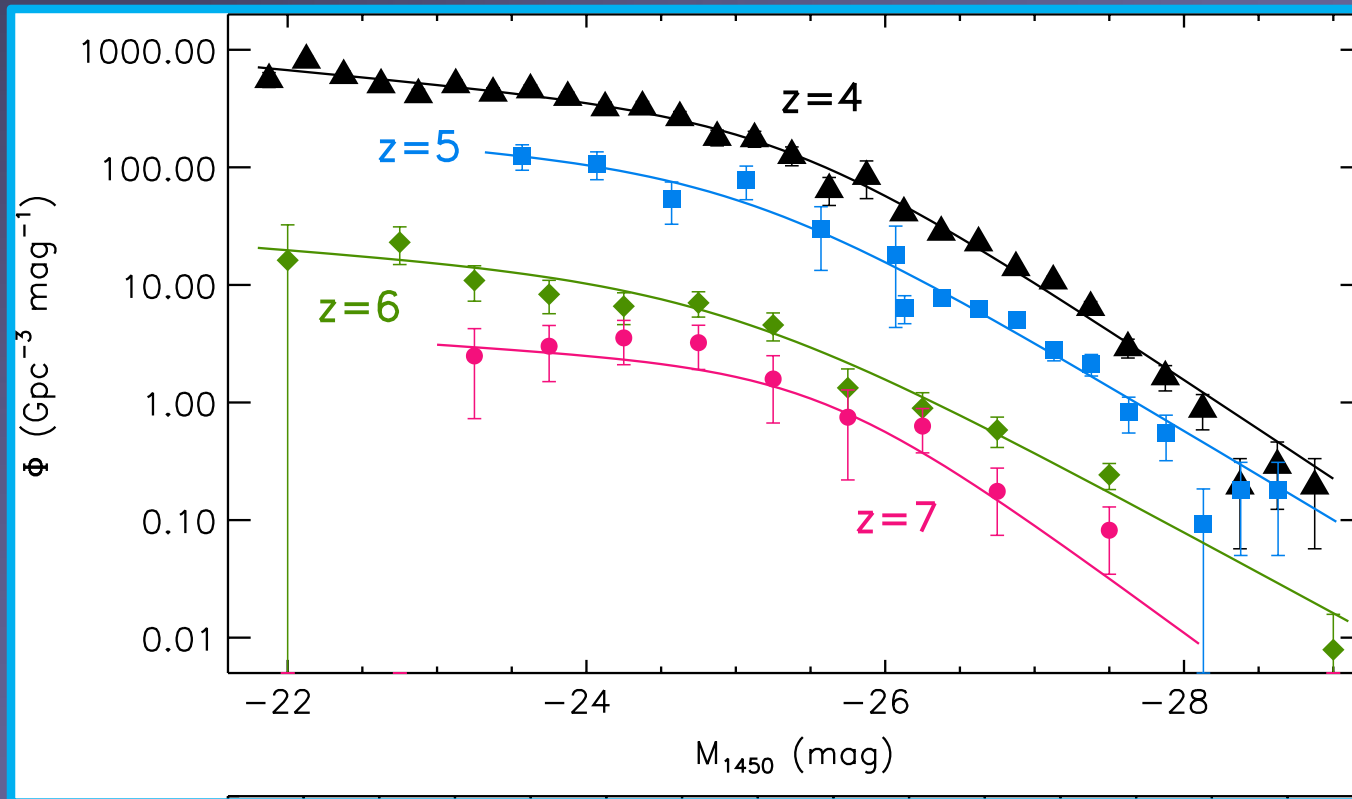
BH

A black hole (BH) is depicted at the center of a glowing accretion disk. The disk is composed of concentric rings of gas and dust, glowing with intense red and orange light. The background is a dark, starry space.

Accretion disk

Evolution of Massive BHs in Nuclei

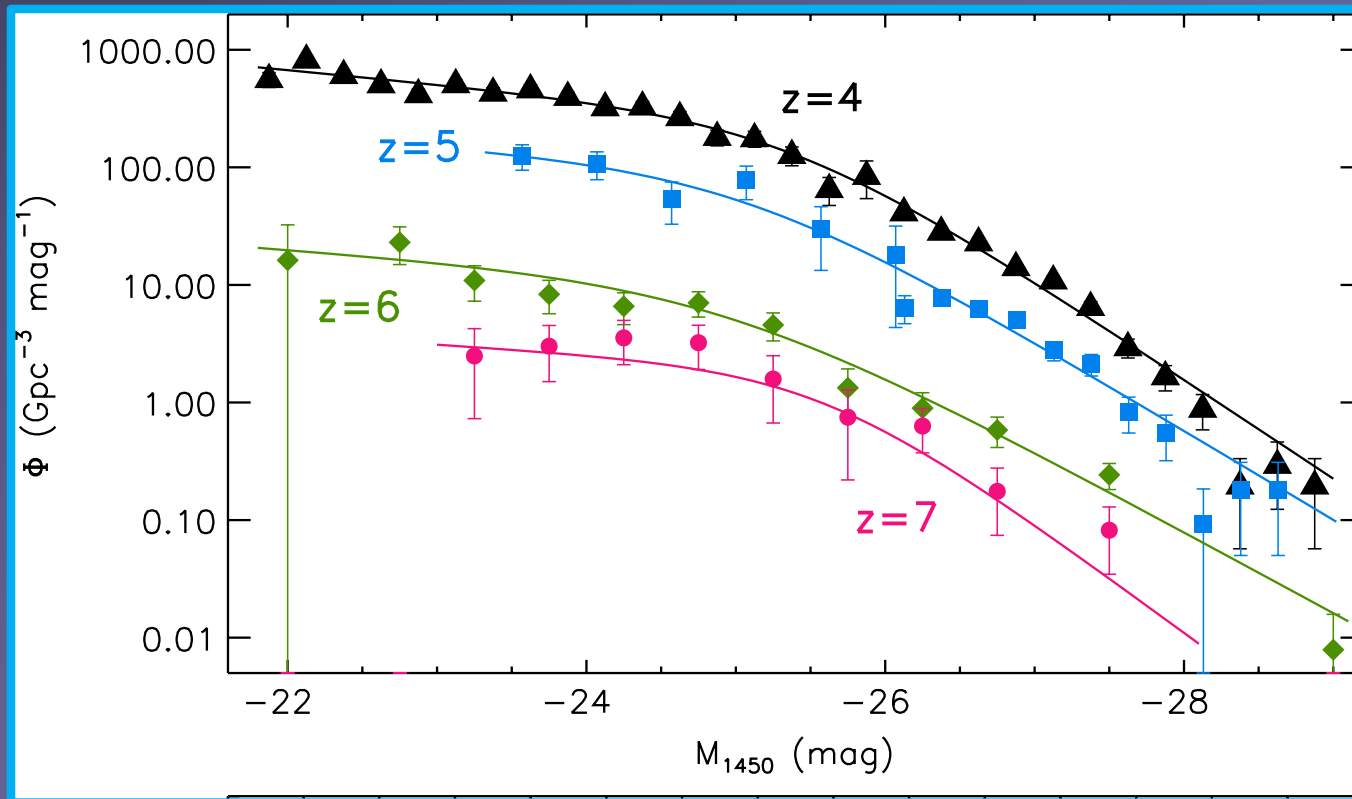
Quasars with $M_{\text{BH}} = 10^{8-10} M_{\odot}$ seen out to $z=7.54$ ($t=700$ Myr)



Matsuoka et al.(2023; arXiv:2305.11225)

Evolution of Massive BHs in Nuclei

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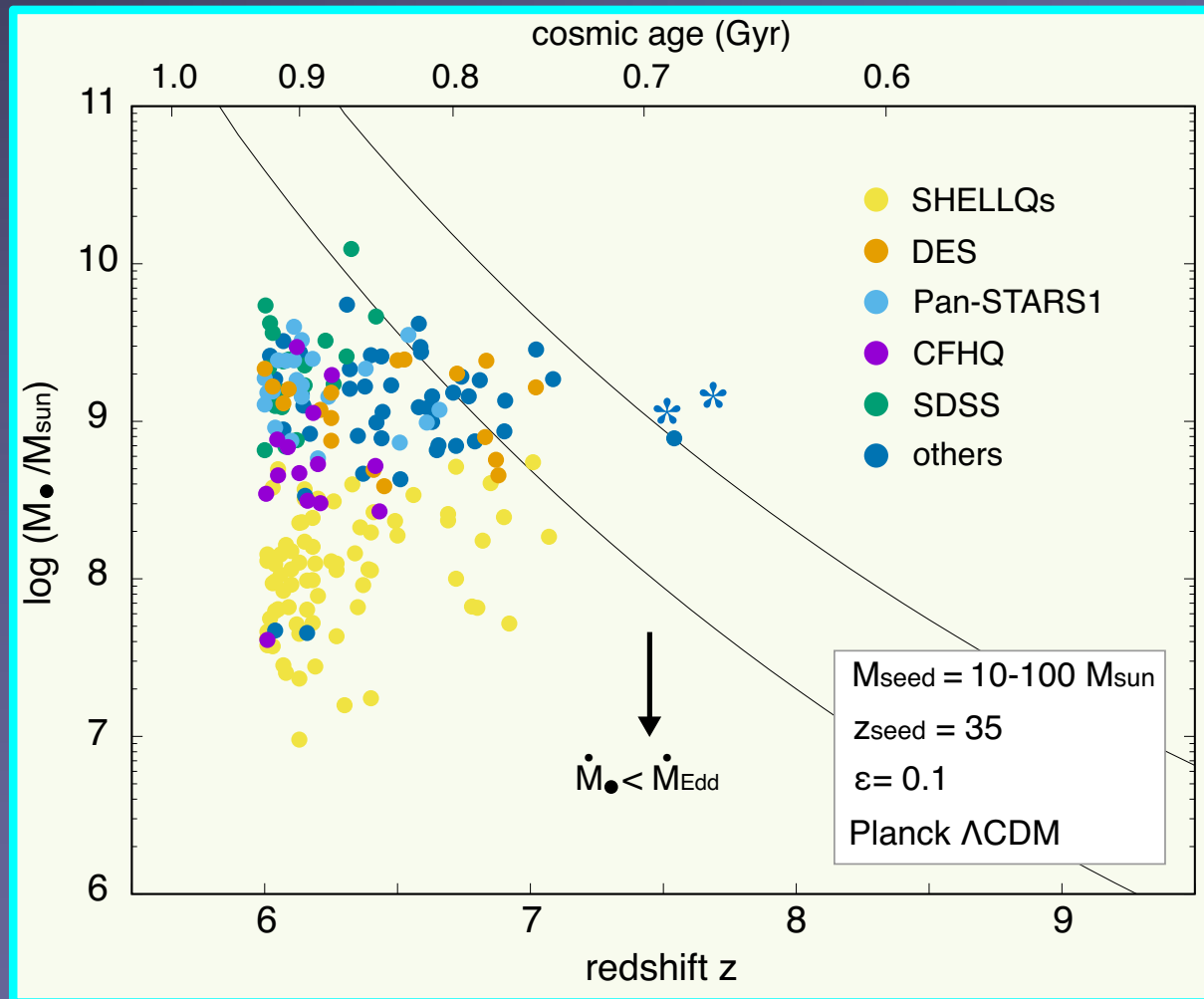
Matsuoka et al.(2023; arXiv:2305.11225)

$\sim 10^6 M_{\odot}$ seeds old: evolution at $z < 6$ ($t > 1$ Gyr) understood from quasars: $L_{\text{Q}} = \epsilon / (1 - \epsilon) dM_{\text{BH}} / dt$ with $\epsilon \sim 10\%$ (Soltan 1991)

The most distant quasars

— distance —→

↑
mass
↓



Record holder:

$z=7.64$

$t=670 \text{ Myr}$

$M=1.6 \times 10^9 M_{\odot}$

Wang+2021

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How to make massive black holes (fast)?

- Method 1: Collapse gas directly into a massive BH
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How to make massive black holes (fast)?



THINK HARDER

Solution

Conditions in early universe different from present-day

densities much higher

myriad of small protogalaxies formed very early

gas chemically primitive

First “galaxies”

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 - Must deflate its pressure not to remain a cloud
 - radiation via collisional excitations of molecules
 - Today: CO, H₂O (T=5K)



PERIODIC TABLE OF THE ELEMENTS

<http://www.ktf-split.hr/periodni/en/>

GROUP	PERIODIC TABLE OF THE ELEMENTS																18		
1	IA										IIA						18		
PERIOD	1	2	3										4	5	6	7	8	9	10
1	1 1.0079 H HYDROGEN	2 4.0026 He HELIUM																	
2	3 6.941 Li LITHIUM	4 9.0122 Be BERYLLIUM	5 10.811 B BORON										6 12.011 C CARBON	7 14.007 N NITROGEN	8 15.999 O OXYGEN	9 18.998 F FLUORINE	10 20.180 Ne NEON		
3	11 22.990 Na SODIUM	12 24.305 Mg MAGNESIUM	13 26.982 Al ALUMINIUM										14 28.086 Si SILICON	15 30.974 P PHOSPHORUS	16 32.065 S SULPHUR	17 35.453 Cl CHLORINE	18 39.948 Ar ARGON		
4	19 39.098 K POTASSIUM	20 40.078 Ca CALCIUM	21 44.956 Sc SCANDIUM	22 47.867 Ti TITANIUM	23 50.942 V VANADIUM	24 51.996 Cr CHROMIUM	25 54.938 Mn MANGANESE	26 55.845 Fe IRON	27 58.933 Co COBALT	28 58.693 Ni NICKEL	29 63.546 Cu COPPER	30 65.39 Zn ZINC	31 69.723 Ga GALLIUM	32 72.64 Ge GERMANIUM	33 74.922 As ARSENIC	34 78.96 Se SELENIUM	35 79.904 Br BROMINE	36 83.80 Kr KRYPTON	
5	37 85.468 Rb RUBIDIUM	38 87.62 Sr STRONTIUM	39 88.906 Y YTTRIUM	40 91.224 Zr ZIRCONIUM	41 92.906 Nb NIOBIUM	42 95.94 Mo MOLYBDENUM	43 (98) Tc TECHNETIUM	44 101.07 Ru RUTHENIUM	45 102.91 Rh RHODIUM	46 106.42 Pd PALLADIUM	47 107.87 Ag SILVER	48 112.41 Cd CADMIUM	49 114.82 In INDIUM	50 118.71 Sn TIN	51 121.76 Sb ANTIMONY	52 127.60 Te TELLURIUM	53 126.90 I IODINE	54 131.29 Xe XENON	
6	55 132.91 Cs CAESIUM	56 137.33 Ba BARIUM	57-71 La-Lu Lanthanide	72 178.49 Hf HAFNIUM	73 180.95 Ta TANTALUM	74 183.84 W TUNGSTEN	75 186.21 Re RHENIUM	76 190.23 Os OSMIUM	77 192.22 Ir IRIDIUM	78 195.08 Pt PLATINUM	79 196.97 Au GOLD	80 200.59 Hg MERCURY	81 204.38 Tl THALLIUM	82 207.2 Pb LEAD	83 208.98 Bi BISMUTH	84 (209) Po POLONIUM	85 (210) At ASTATINE	86 (222) Rn RADON	
7	87 (223) Fr FRANCIUM	88 (226) Ra RADIUM	89-103 Ac-Lr Actinide	104 (261) Rf RUTHERFORDIUM	105 (262) Db DUBNIUM	106 (266) Sg SEABORGIUM	107 (264) Bh BOHRIUM	108 (277) Hs HASSIUM	109 (268) Mt MEITNERIUM	110 (281) Uun UNUNNIUM	111 (272) Uuu UNUNUNIUM	112 (285) Uub UNUNBIUM	114 (289) Uuq UNUNQUADIUM						

RELATIVE ATOMIC MASS (1)

GROUP IUPAC GROUP CAS

ATOMIC NUMBER SYMBOL ELEMENT NAME

■ Metal ■ Semimetal ■ Nonmetal
1 Alkali metal 16 Chalcogens element
2 Alkaline earth metal 17 Halogens element
3-10 Transition metals 18 Noble gas
11-17 Lanthanide
8-10 Actinide

STANDARD STATE (25 °C; 101 kPa)

■ Ne - gas ■ Fe - solid
■ Ga - liquid ■ Tc - synthetic

(1) Pure Appl. Chem., 73, No. 4, 667-683 (2001)
 Relative atomic mass is shown with five significant figures. For elements having no stable nuclides, the value enclosed in brackets indicates the mass number of the longest-lived isotope of the element.
 However three such elements (Th, Pa, and U) do have a characteristic terrestrial isotopic composition, and for these an atomic weight is tabulated.

LANTHANIDE

57 138.91 La LANTHANUM	58 140.12 Ce CERIUM	59 140.91 Pr PRASEODYMIUM	60 144.24 Nd NEODYMIUM	61 (145) Pm PROMETHIUM	62 150.36 Sm SAMARIUM	63 151.96 Eu EUROPIUM	64 157.25 Gd GADOLINIUM	65 158.93 Tb TERBIUM	66 162.50 Dy DYSPROSIUM	67 164.93 Ho HOLMIUM	68 167.26 Er ERBIUM	69 168.93 Tm THULIUM	70 173.04 Yb YTTERBIUM	71 174.97 Lu LUTETIUM
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ACTINIDE

89 (227) Ac ACTINIUM	90 232.04 Th THORIUM	91 231.04 Pa PROTACTINIUM	92 238.03 U URANIUM	93 (237) Np NEPTUNIUM	94 (244) Pu PLUTONIUM	95 (243) Am AMERICIUM	96 (247) Cm CURIUM	97 (247) Bk BERKELIUM	98 (251) Cf CALIFORNIUM	99 (252) Es EINSTEINIUM	100 (257) Fm FERMIUM	101 (258) Md MENDELEVIUM	102 (259) No NOBELIUM	103 (262) Lr LAWRENCIUM
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PERIODIC TABLE OF THE ELEMENTS IN THE EARLY UNIVERSE

	GROUP	
	1	IA
PERIOD	1	1.0079
1	H	
	HYDROGEN	

	18	VIIIA
2	4.0026	
	He	
	HELIUM	

First “galaxies”

- First “galaxies” appear at 100 million years
 - Gravity has to overcome gas pressure (“Jeans mass”)
 - First “micro-galaxies” contain $10^6 M_{\odot}$ of gas

- First stars and black holes?
 - Must deflate its pressure not to be stuck as a cloud
 - radiation via excitations of molecules
 - Today: CO, H₂O (T=5K)



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 - Protogalaxies with H₂ : $T=100 K$
 - Protogalaxies with only H atoms: $T=10^4 K$



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H₂ molecule controls fate of first stars/BHs

H₂ abundance depends on local radiation



- Formation:



- Destruction:



Strong Lyman-Werner radiation ($\sim 12\text{eV}$)
suppresses H₂ fraction and cooling
Jemma Wolcott-Green (PhD thesis 2019)

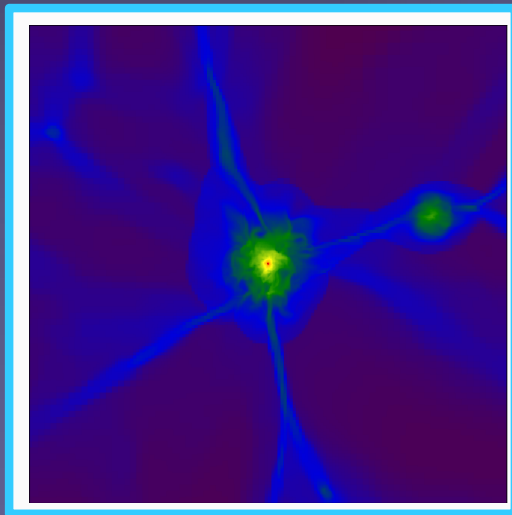
Realized in **synchronized formation of a pair of protogalaxies**
 $\Delta t_{\text{sync}} < 4 \text{ Myr}$ and $d_{\text{sep}} < 1000 \text{ light-yr}$ in $\sim 10^{-4}$ of protogalaxies

3D simulation of protogalaxy collapse

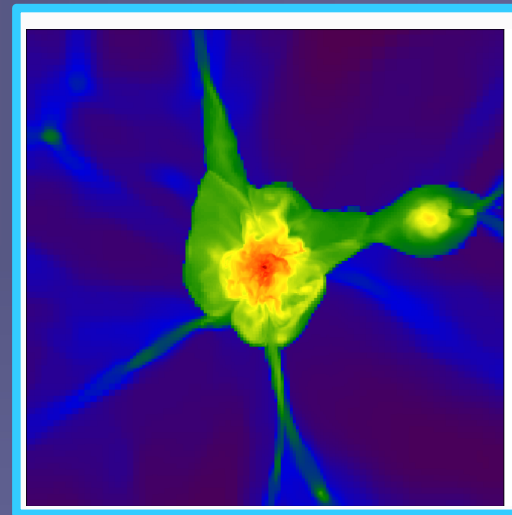
- no free parameters -

$$M_{\text{galaxy}} \approx 10^{6-8} M_{\odot} \quad t_{\text{coll}} \approx 300 \text{ Myr}$$

Fernandez et al. (2014), Regan et al. (2017)



density



temperature

Inflow rate **increases** with temperature

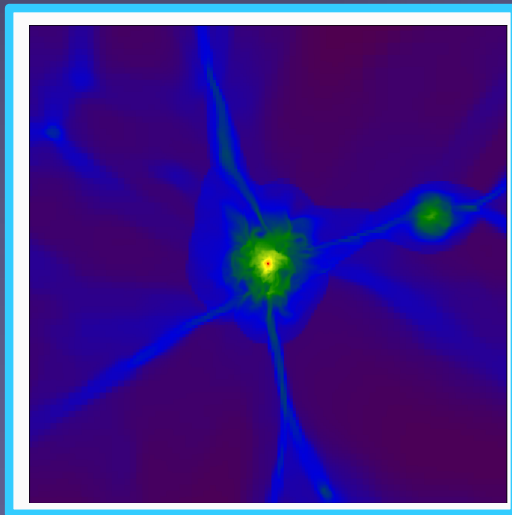
$$dM/dt \sim c_s^3 / G \sim T^{3/2} / G$$

~~3D simulation~~ of protogalaxy collapse calculation

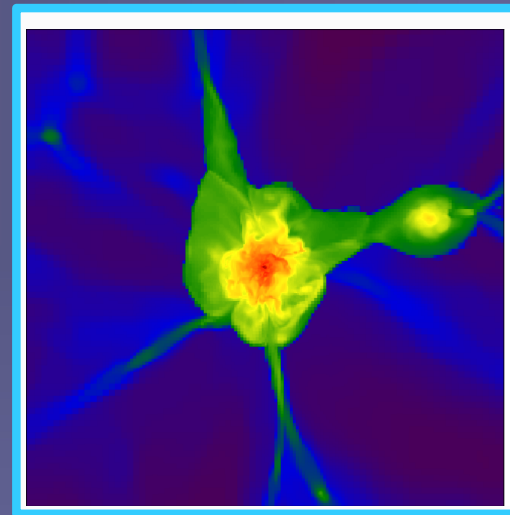
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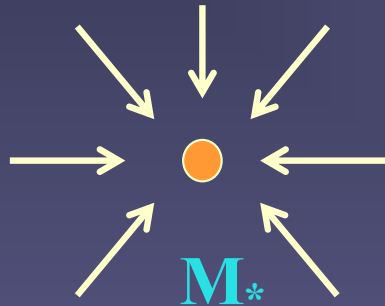


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What happens in the (unresolved) core?



present-day galaxy
abundant $\text{CO}, \text{H}_2\text{O}$

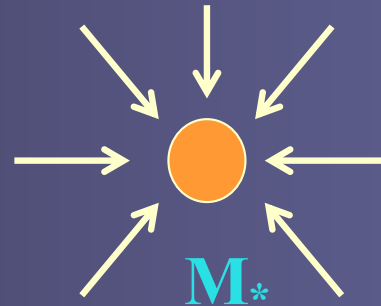
$$T \approx 5 \text{ K}$$

$$\dot{M} \approx 10^{-5} M_{\odot} \text{ yr}^{-1}$$

result: a star

$$M_* \approx 1-10 M_{\odot}$$

0.1% chance of BH



$10^6 M_{\odot}$ protogalaxy
abundant H_2

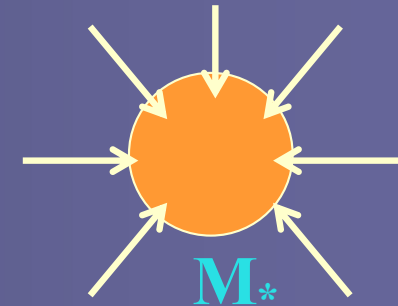
$$T \approx 200 \text{ K}$$

$$\dot{M} \approx 10^{-3} M_{\odot} \text{ yr}^{-1}$$

result: massive star

$$M_* \approx 10-500 M_{\odot}$$

50% chance of BH



$10^8 M_{\odot}$ protogalaxy
no H_2 - cooling by H

$$T \approx 10,000 \text{ K}$$

$$\dot{M} \approx 1 M_{\odot} \text{ yr}^{-1}$$

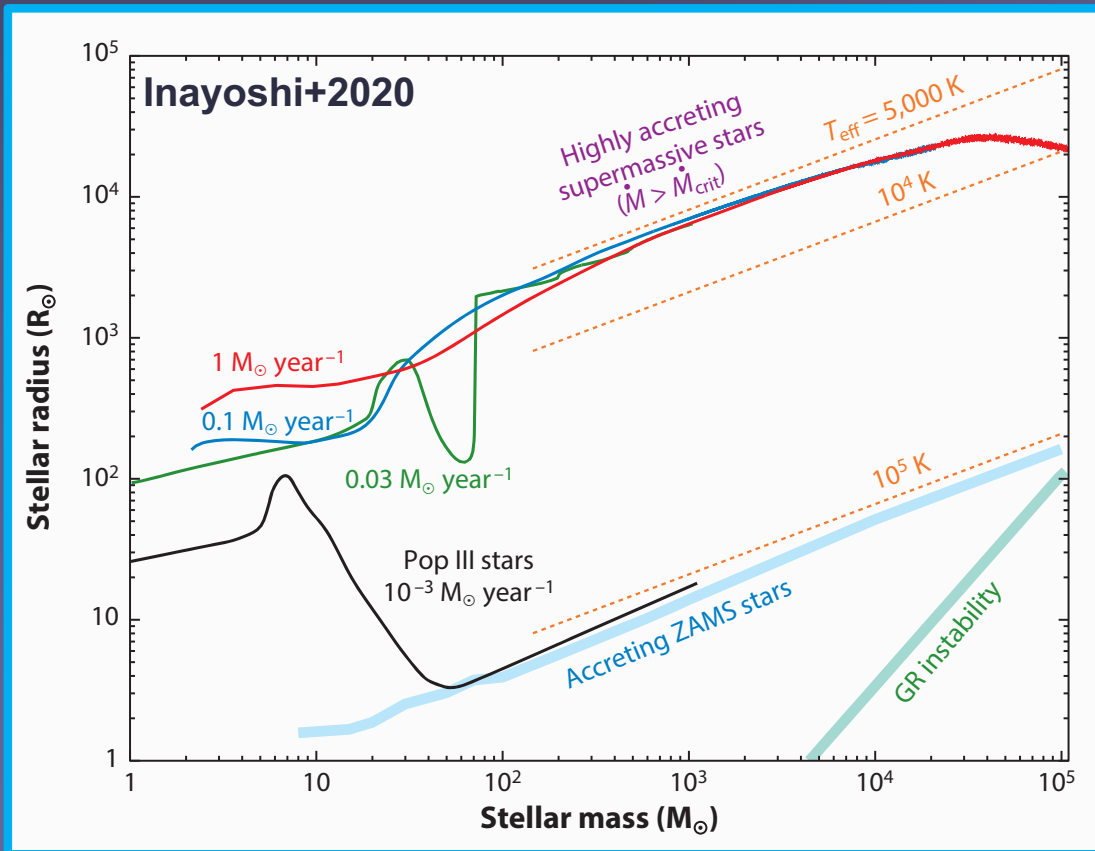
supermassive star

$$M_* \approx 10^{5-6} M_{\odot}$$

→ Massive BH

Direct collapse

- Protostar must be building up faster than it can contract (Kelvin-Helmholtz timescale $\sim 10^4$ years)
- Leave behind massive $10^5\text{-}6 M_\odot$ BHs via GR instability



Hosokawa et al. 2012, 2015; Haemmerlé et al. 2018

SMS: achieved by rapid gas accretion

Normal star: $M \gtrsim 10^3 M_\odot$ prevented by UV radiation

isothermal collapse via Ly α cooling:

$$M_{\text{acc}} \approx c_s^3 / G \approx 0.1\text{-}1 M_\odot \text{yr}^{-1}$$

cf. inflow rate with H₂ cooling:

$$c_s^3 / G \approx 10^{-3} M_\odot \text{yr}^{-1}$$

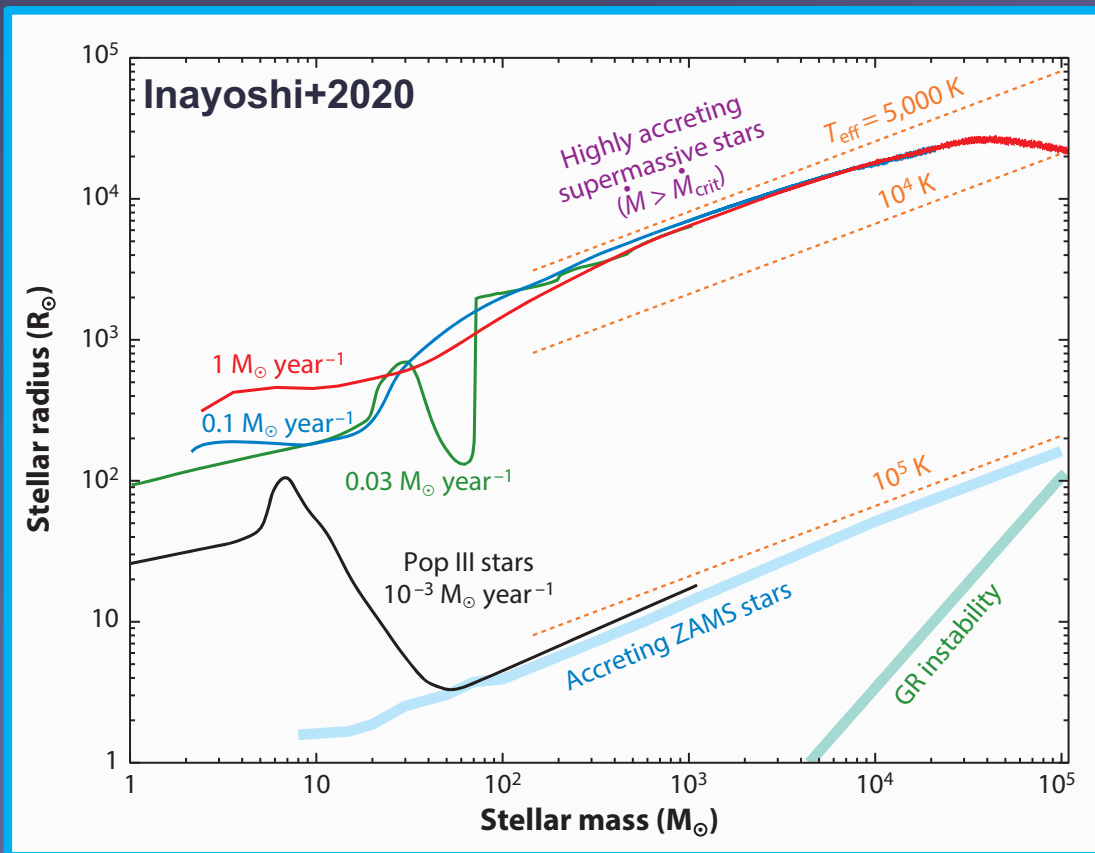
cf. molecular clouds in ISM:

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Direct collapse

(rapid inflow \rightarrow supermassive star \rightarrow MBH)

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- Method 1: Collapse gas directly into a massive BH
problem: cloud fragments and forms stars
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problem: accretion rate low
- Method 3: Merge together many black holes
problem: too few mergers

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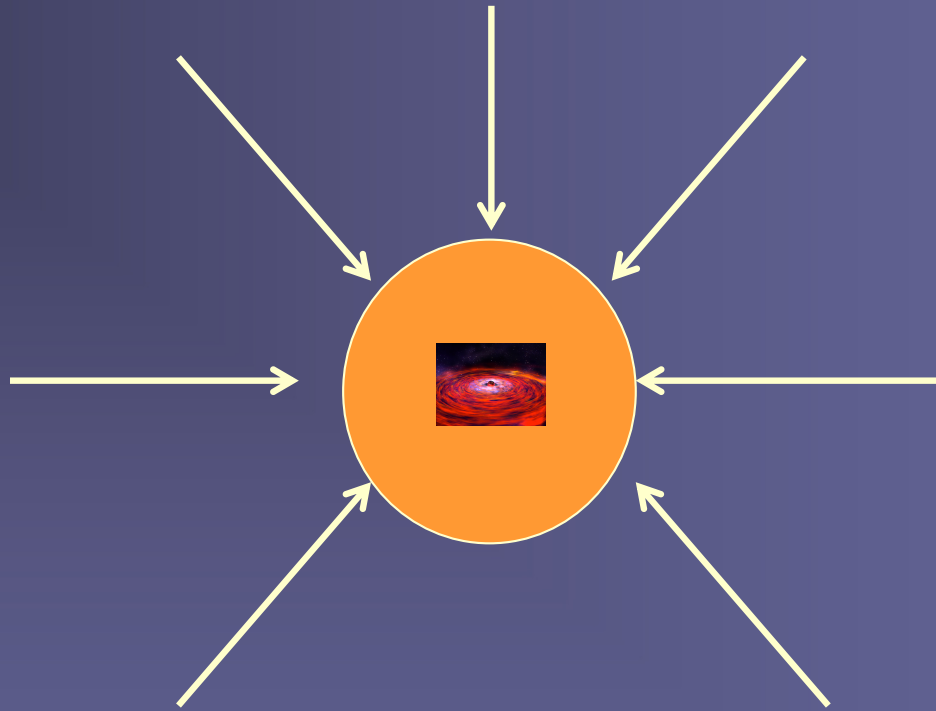
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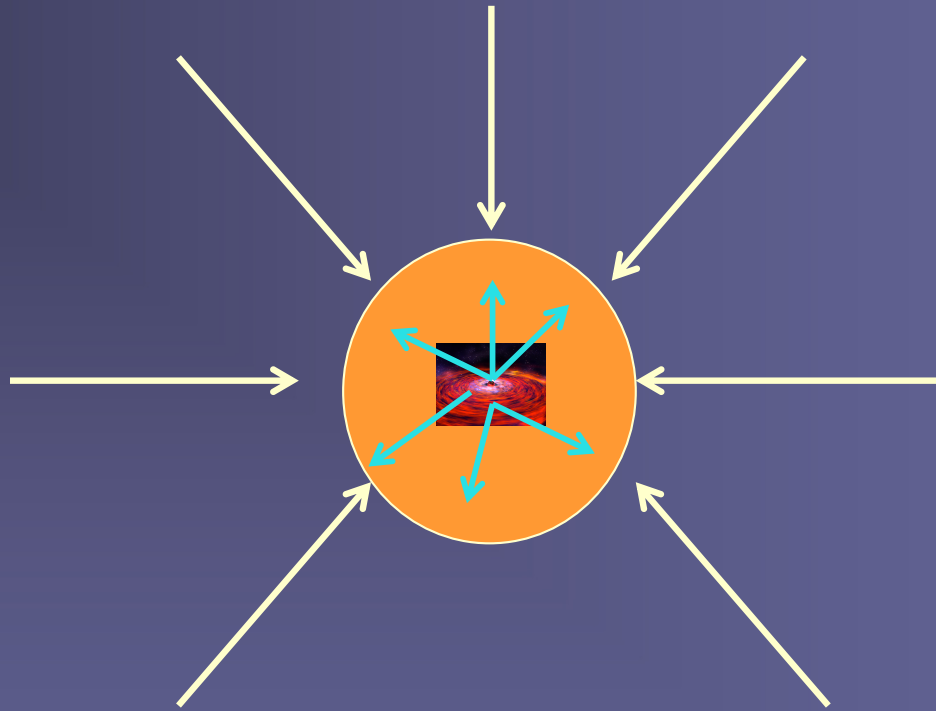
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Feeding Black Holes



Feeding Black Holes



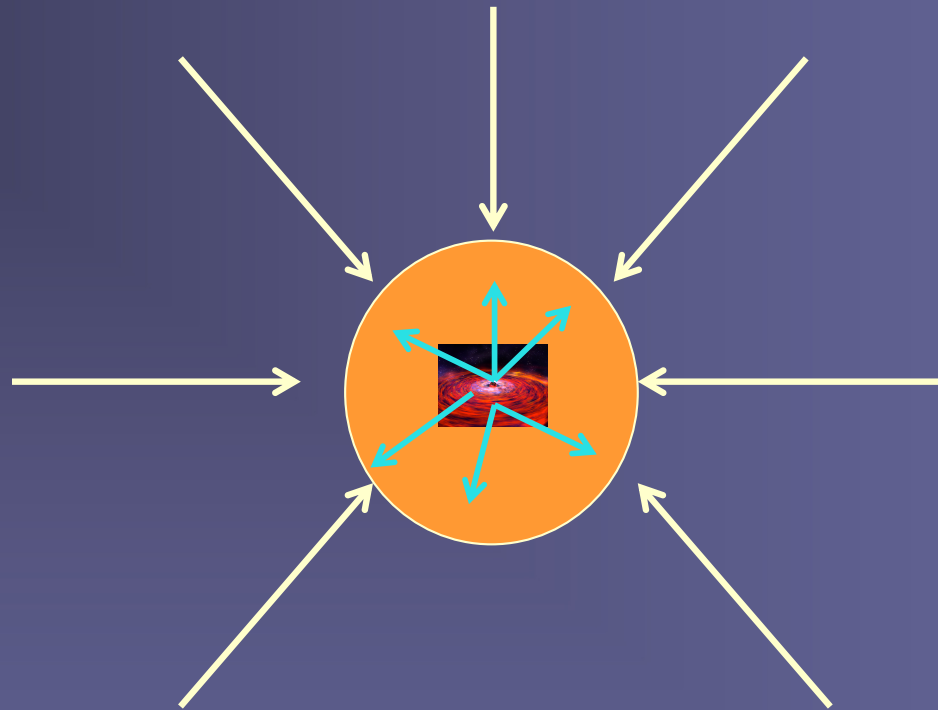
inward
gravity

vs

outward
radiation

$$L \sim GM_{bh} \dot{M}_{bh} / R_{bh}$$

Feeding Black Holes



inward
gravity

vs

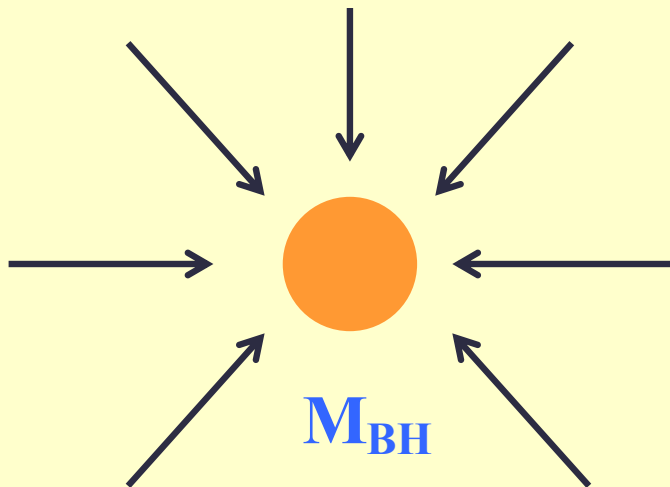
outward
radiation

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there is a
universal
maximum
“Eddington”
feeding rate

Maximum Growth Rate and BH mass



Fueling rate:

$$\frac{dM_{gas}}{dt}$$

BH growth rate:

$$\frac{dM_{BH}}{dt} = \epsilon \frac{dM_{gas}}{dt}$$

BH luminosity:

$$L_{BH} = (1 - \epsilon) \frac{dM_{gas} c^2}{dt}$$

Outward force:

$$F_{rad} = const \times \frac{L_{BH}}{4\pi r^2} = const \times \frac{\dot{M}_{BH}}{r^2}$$

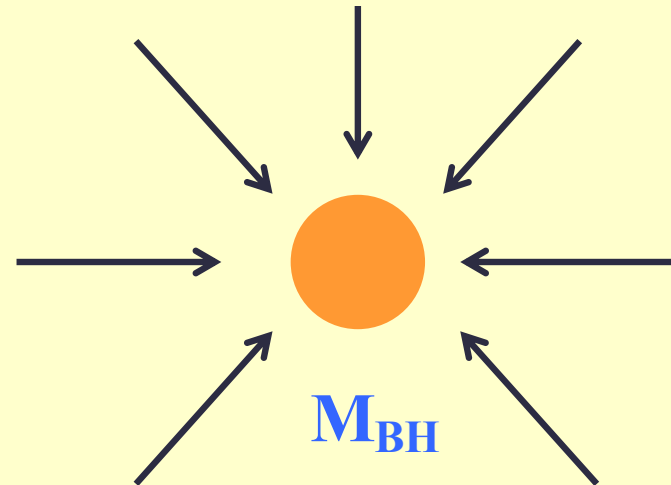
$$L_{BH} = \frac{(1 - \epsilon)}{\epsilon} \frac{dM_{BH} c^2}{dt}$$

Maximum growth rate:

$$F_{rad} = F_{grav} = \frac{GM_{BH}}{r^2} \quad \rightarrow \quad \dot{M}_{BH,MAX} = const \times M_{BH}$$

$$M_{BH}(t) = ???$$

Maximum Growth Rate and BH mass

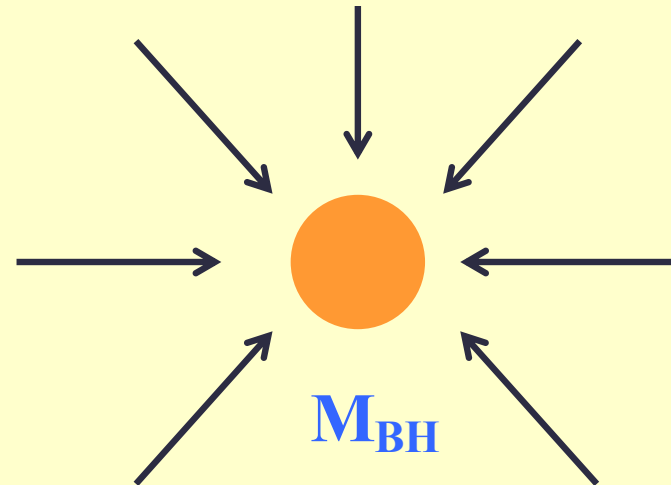


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Maximum Growth Rate and BH mass



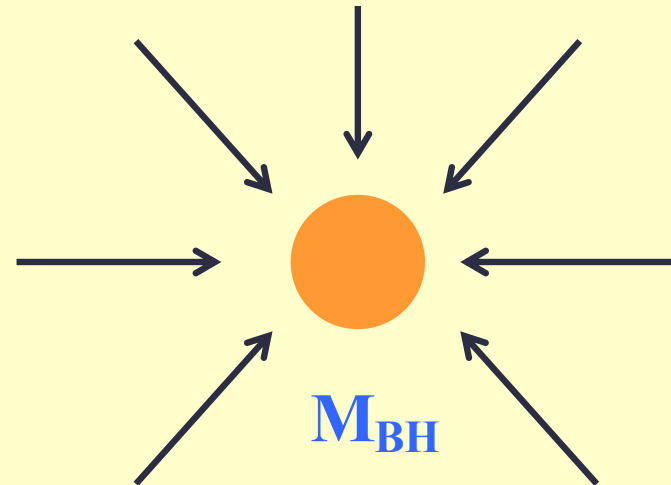
Maximum growth rate:

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→

$$M_{BH}(t) = M_{BH}(t=0) \times \exp\left(\frac{t}{T}\right)$$

Maximum Growth Rate and BH mass



Maximum growth rate:

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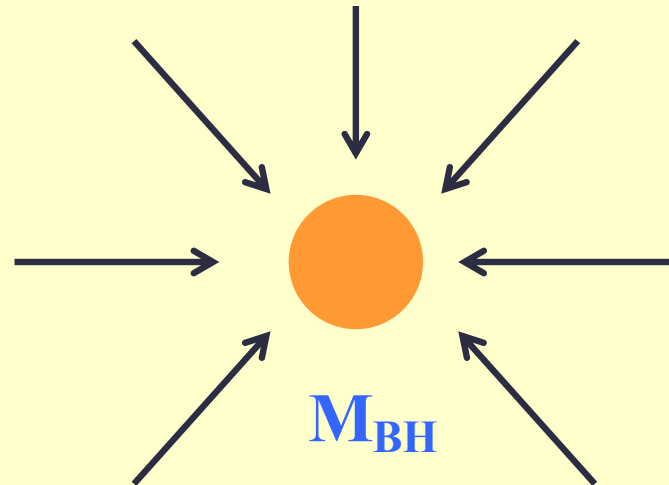
→ $M_{BH}(t) = M_{BH}(t=0) \times \exp\left(\frac{t}{T}\right)$

Massive star: $100 M_{\odot}$

~ 40 million years

700
million
years

Maximum Growth Rate and BH mass



Maximum growth rate:

$$\dot{M}_{BH,MAX} = const \times M_{BH}$$

$$\rightarrow M_{BH}(t) = M_{BH}(t=0) \times \exp\left(\frac{t}{T}\right)$$

700
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years

Massive star: $100 M_{\odot}$

~ 40 million years

\rightarrow Maximum $M_{BH} = 10^8 M_{\odot}$ too small!

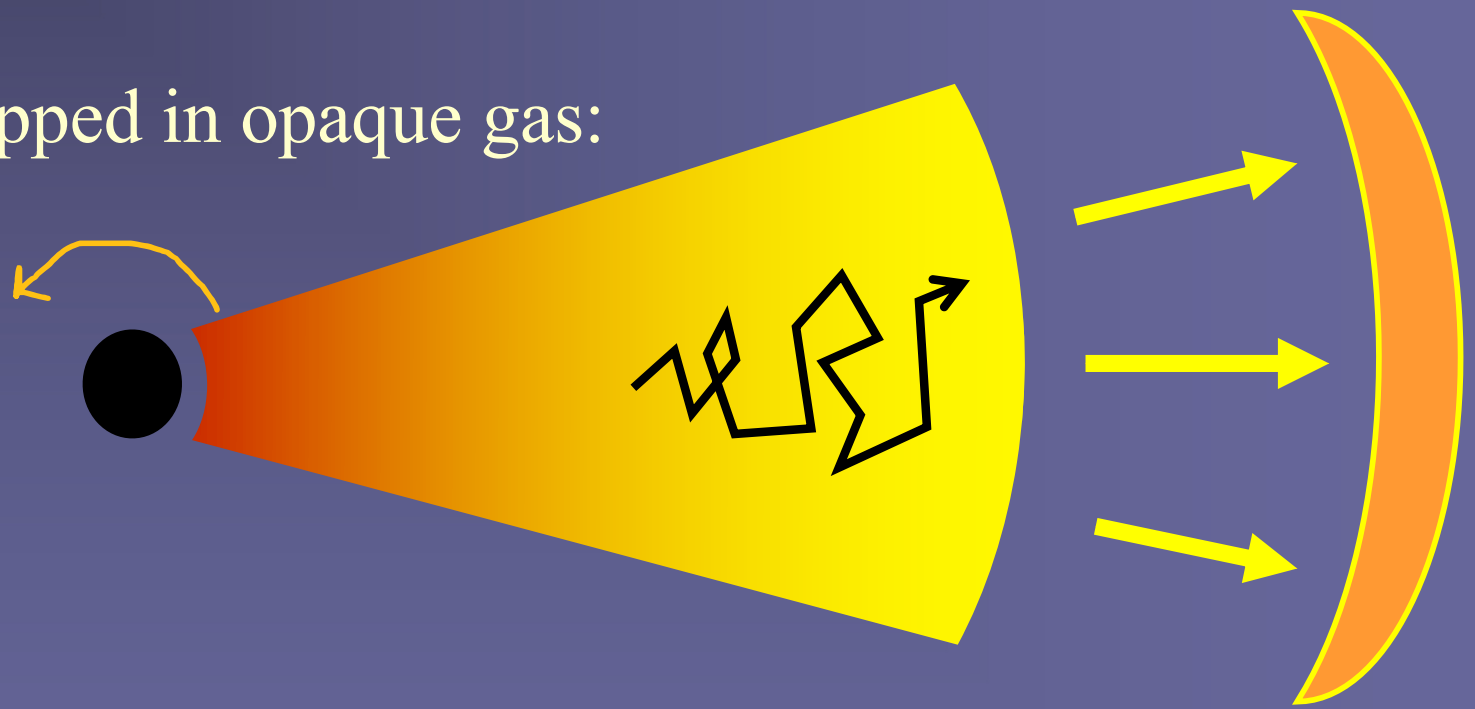
Hyper-accretion onto BH

Spherically symmetric radiation + hydrodynamics simulations

Inayoshi, ZH, Ostriker (2016), Sakurai, Inayoshi, ZH (2017), Hu et al. (2022a,b)

I. Radiation trapped in opaque gas:

$$L \sim GM_{bh} \dot{M}_{bh} / R_{bh}$$



Hyper-accretion onto BH

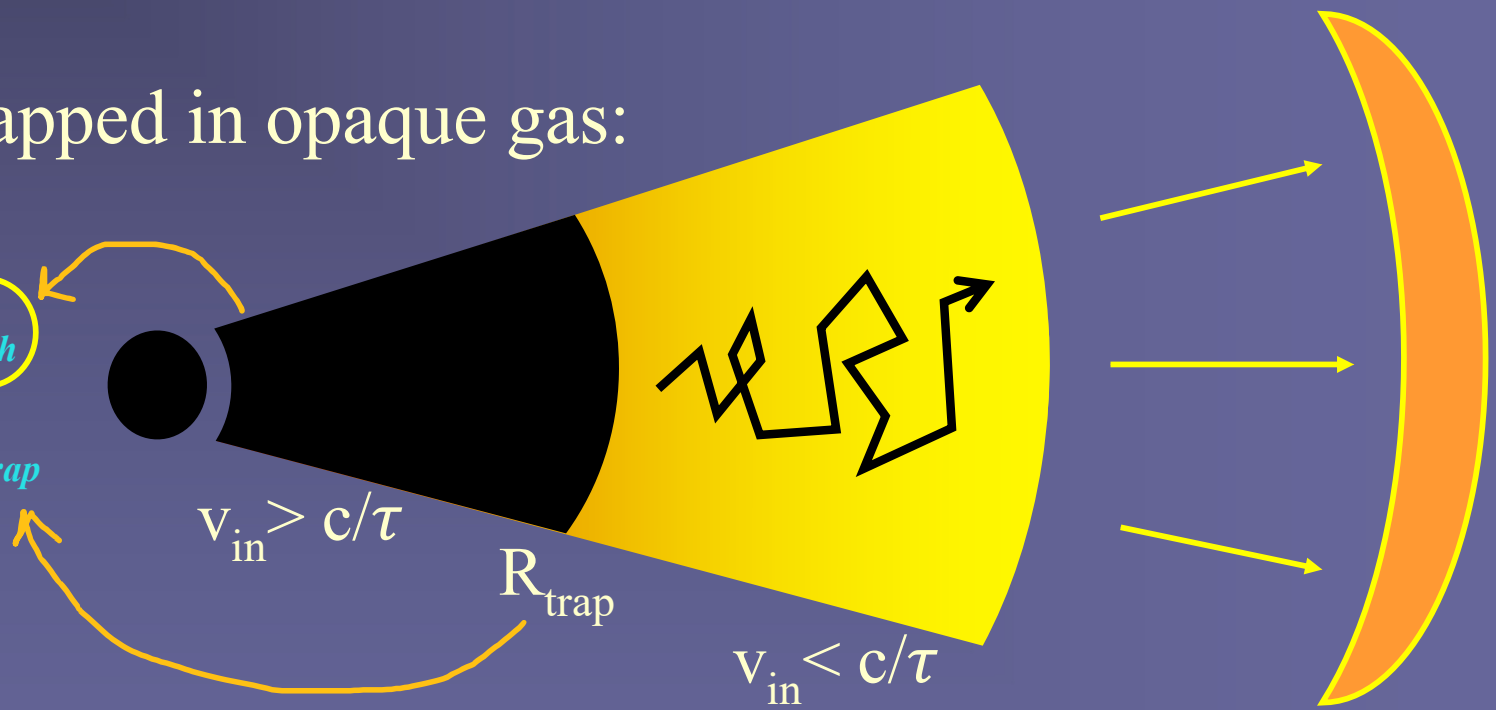
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$$L \sim GM_{bh} \dot{M}_{bh} / R_{trap}$$



Hyper-accretion onto BH

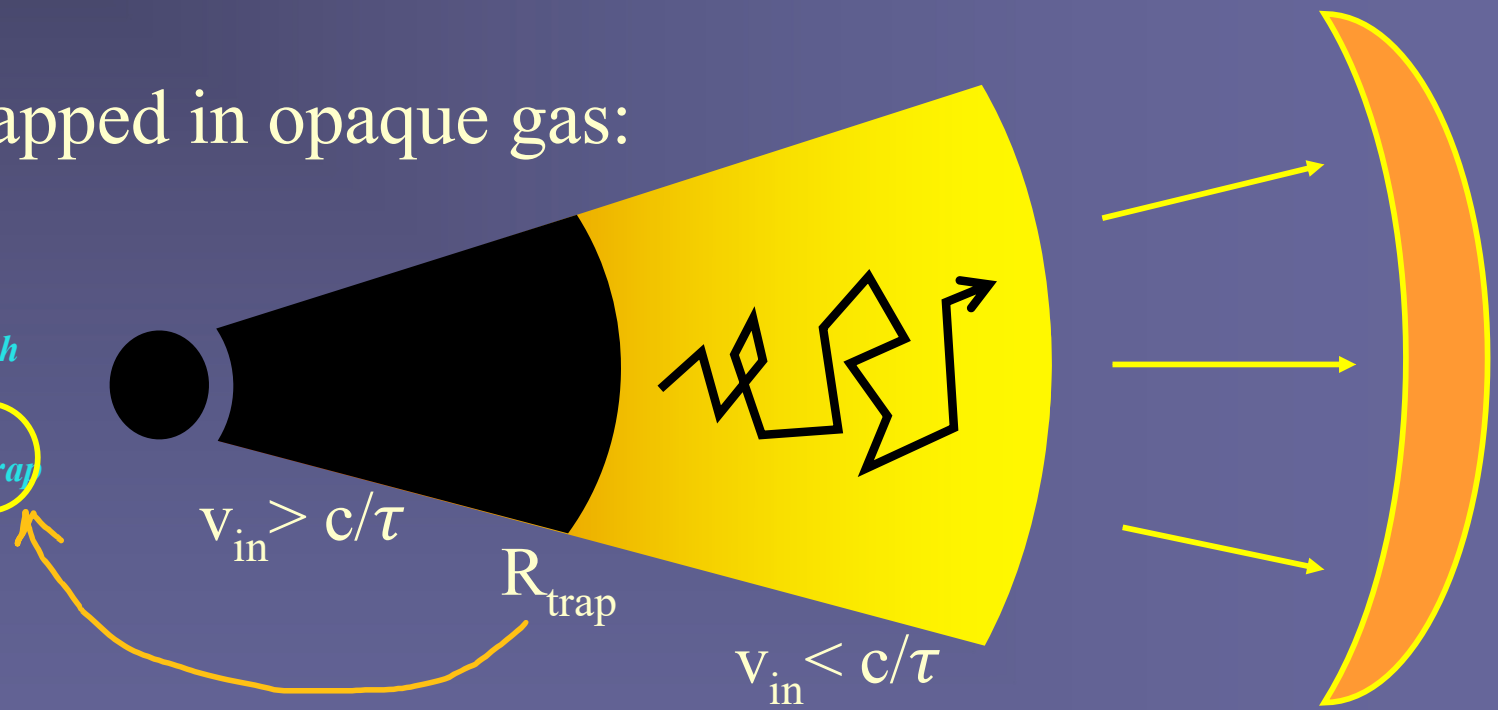
Spherically symmetric radiation + hydrodynamics simulations

Inayoshi, ZH, Ostriker (2016), Sakurai, Inayoshi, ZH (2017), Hu et al. (2022a,b)

I. Radiation trapped in opaque gas:

$$L \sim G\dot{M}_{bh}M_{bh}/R_{bh}$$

$$L \sim G\dot{M}_{bh}M_{bh}R_{trap}$$



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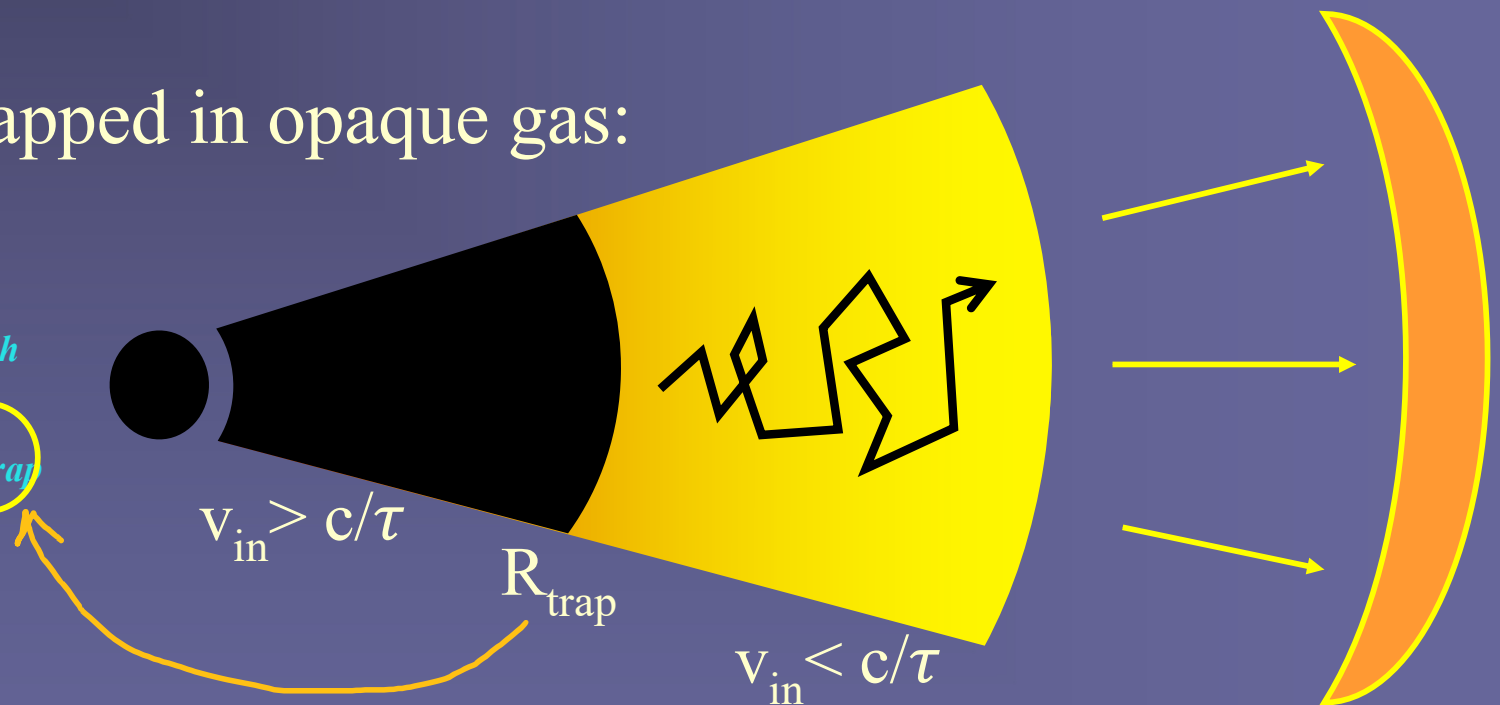
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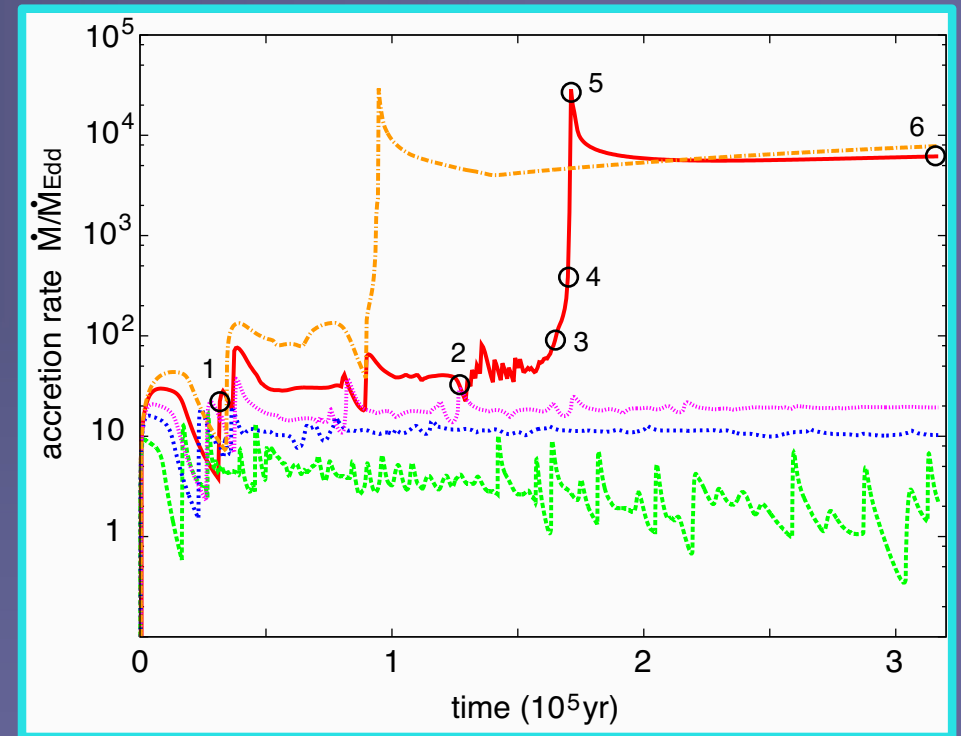
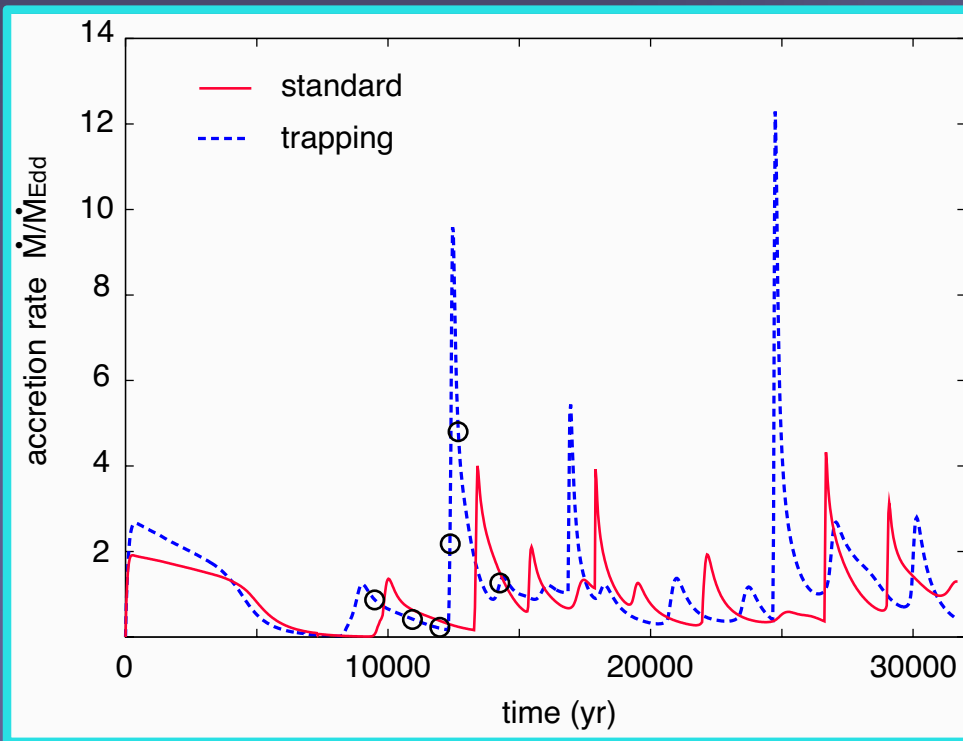
II. If fueling is extremely rapid ($\gtrsim 500 \times$ Eddington rate) then emerging radiation cannot stop inflow: the BH swallows everything (otherwise, episodic accretion)

Hyper-accretion onto BH

1D and 2D radiation + hydrodynamics simulations

$$\dot{M} = 100 \dot{M}_{\text{Edd}}$$

$$\dot{M} = 10^4 \dot{M}_{\text{Edd}}$$



Accretion episodic due to heating
average rate is very low
(sub-Eddington)

Accretion is steady
matches feeding rate
(gas free-falls onto BH)

Toy model for steady hyper-accretion

Sakurai, Inayoshi & ZH (2017)

- Infalling gas neutral \rightarrow Eddington luminosity irrelevant
- Consider a toy model: geometrically thin, optically thick spherical shell around a point source, driven by radiation force into a rapidly collapsing medium



$$\frac{d}{dt}(M_{\text{sh}} \dot{R}_{\text{sh}}) = \frac{L}{c} - \dot{M}(|v| + \dot{R}_{\text{sh}}) - \frac{GM_{\text{BH}}M_{\text{sh}}}{R_{\text{sh}}^2}$$

$$\frac{dM_{\text{sh}}}{dt} = \dot{M} \left(1 + \frac{\dot{R}_{\text{sh}}}{|v|} \right),$$

How to make massive BHs (fast)?

- Method 1: Collapse gas directly into a massive BH

problem: cloud fragments and forms stars

solution: rapid inflow in large but pristine H_2 -free protogalaxy

- Method 2: Grow a single stellar-mass BH by accretion

problem: accretion rate low

- Method 3: Merge together many black holes

problem: too few mergers

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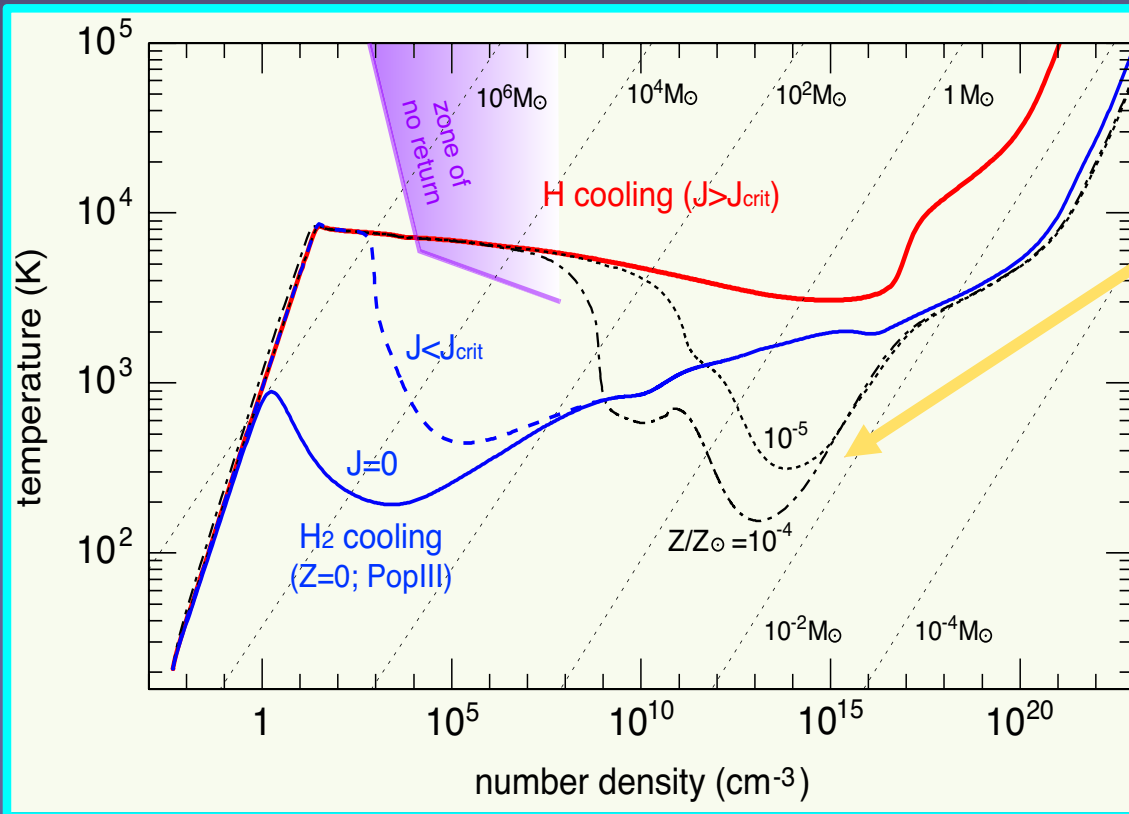
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Runaway Collisions

What happens in atomic-cooling halo if there is prior star-formation and corresponding metal-enrichment? (i.e. in more typical case)

Dense stellar cluster forms \rightarrow core collapse \rightarrow IMBH with 10^3 - $10^4 M_{\odot}$



key: fragmentation at very high density ($\sim 10^{10} M_{\odot} \text{pc}^{-3}$)

- \rightarrow Ultra-dense star cluster
- \rightarrow Runaway core collapse
- \rightarrow VMS
- \rightarrow IMBH

Omukai, ZH, Schneider 2008
 Devecchi & Volonteri 2009
 Katz+2015, Sakurai+2017
 Reinoso+2018, Boekholt+2018
 Alister Seguel+2020, Das+2020

Variant: “Stellar Bombardment”

Tagawa, ZH & Kocsis (2020)

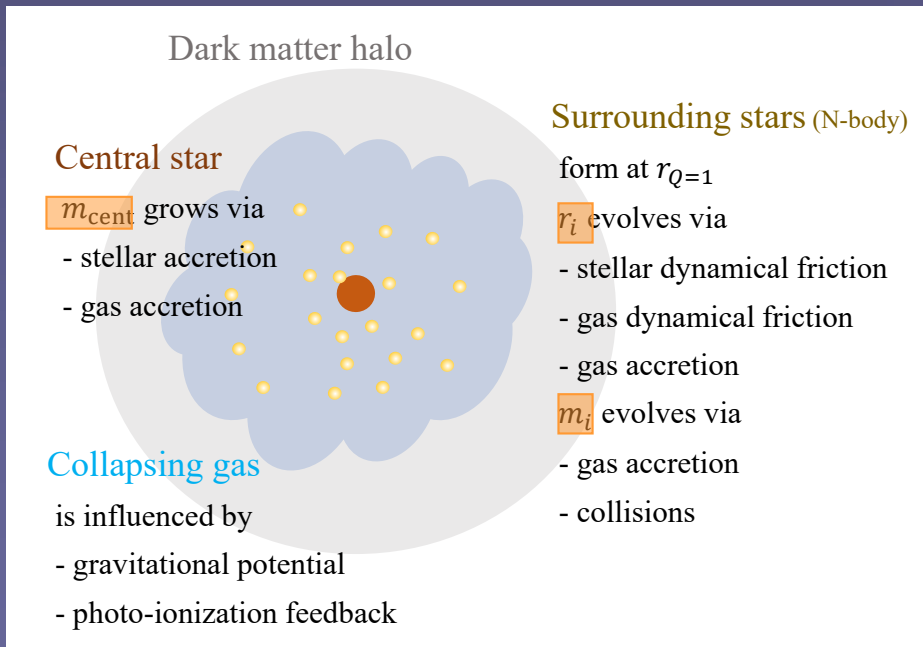
atomic-cooling halo with modest $Z \sim 10^{-4} Z_{\odot}$

Numerical N-body + gas toy model
to follow time-evolution for 3 Myr
 (“1-dimensional N-body simulation”)

Results:

- Central star grows via mergers before it contracts
- Feedback loop: increased radius \leftrightarrow more rapid mergers
- “Bombardment” different from runaway due to mass segregation
- Critical density: $\rho \gtrsim 10^{8-9} M_{\odot} \text{pc}^{-3}$ (cf. $\rho \sim 10^7 M_{\odot} \text{pc}^{-3}$ in M32)

→ SMS with $10^{5-6} M_{\odot}$



BH growth by cosmological *Mergers and Acquisitions*

1 billion yr:

*A single black hole,
with mass of $10^9 M_{\odot}$*



Galaxy merger
tree – follows
from cosmological
theory

The holes grow by
both *accretion* and
by many *mergers*

Many holes are
ejected into space
and lost

100 million yr:

*several hundred
stellar-mass black holes,
each with $100 M_{\odot}$*

← lucky early BH at 60-70 Myr
no recoil -- unequal mass at merger

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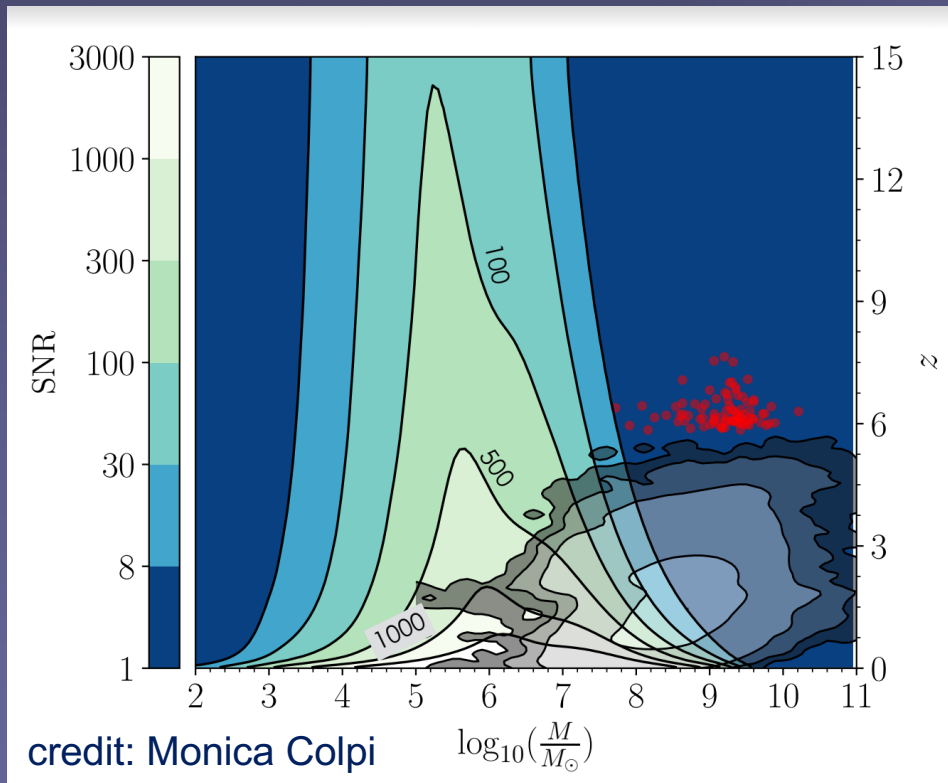
solution: ultra-dense clusters, and/or lucky ultra-early seed

Outline

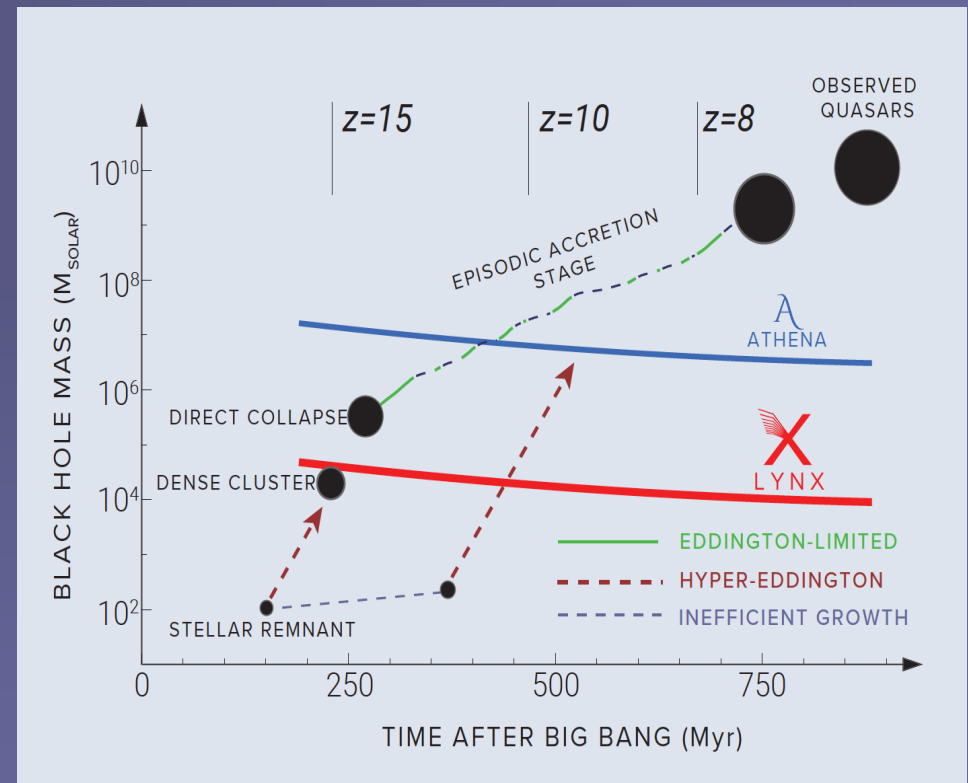
1. Observations: types of black holes in the universe
 2. Theory: where do massive black holes come from?
 3. The Future: how to distinguish different pathways?
-

Looking for early black hole growth

Growth by mergers: LISA



Growth by accretion: LynX



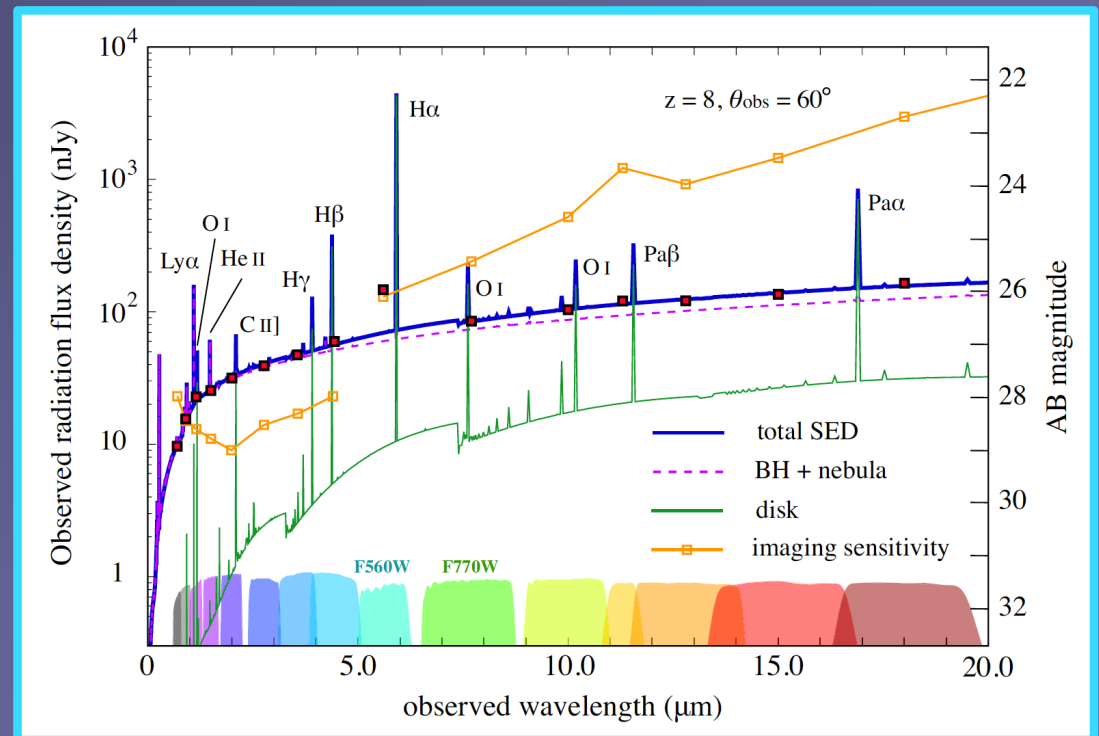
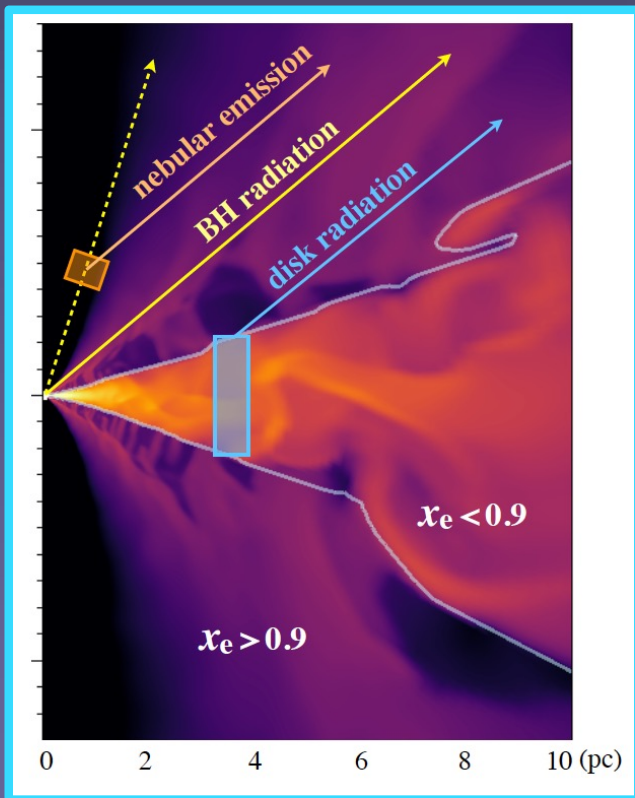
Emerging spectrum

2D radiation-hydro simulations for hyper-accretion

Hu, Inayoshi, ZH, Quataert, Kuiper 2022a; Inayoshi+2022

CLOUDY post-processing of 0.1-100pc around $10^{5-6} M_{\odot}$ BH accreting $1 M_{\odot}/\text{yr}$

$$L_{\text{bol}} \sim 10^{45} \text{ erg/s}$$



rapidly accreting BHs detectable to $z < 17$ or $z < 13$
expected abundance: 1 per 10 NIRCcam fields

Distinguishing signatures

- Strong Balmer lines

collisional excitations of $n \geq 3$ levels from $n=2$ populated by trapped Ly α due to high column density of the dense inner disk (0.1-1 pc)

H α rest-frame EW $\sim 1300 \text{ \AA}$ ($\sim 6-7$ times stronger than low- z quasars)

H β rest-frame EW $\sim 100 \text{ \AA}$ ($\sim 2-3$ times stronger than low- z quasars)

- Red colors in broad bands, due to strong H α

broad-band selection by multiband photometry with NIRCcam & MIRI

$F356W - F560W > 1$ ($7 < z < 8$)

$F444W - F770W > 1$ ($9 < z < 12$)

- OI lines (1304, 8446, 11287 \AA) excited by Ly β fluorescence coinciding with OI 3d (Ly β trapped but OI cascade lines (3d \rightarrow 3p, 3p \rightarrow 3s, 2s \rightarrow 2s) escape detectable by NIRSspec

BH mass to host galaxy mass ratio

Visbal & ZH 2018; Scoggins, ZH & Wise 2023

In rapid formation/growth models, massive BHs are born as **extreme outliers in BH – galaxy mass relation**

Nearby galaxies:

$$M_{\text{bh}}/M_* \sim \text{few} \times 10^{-3}$$

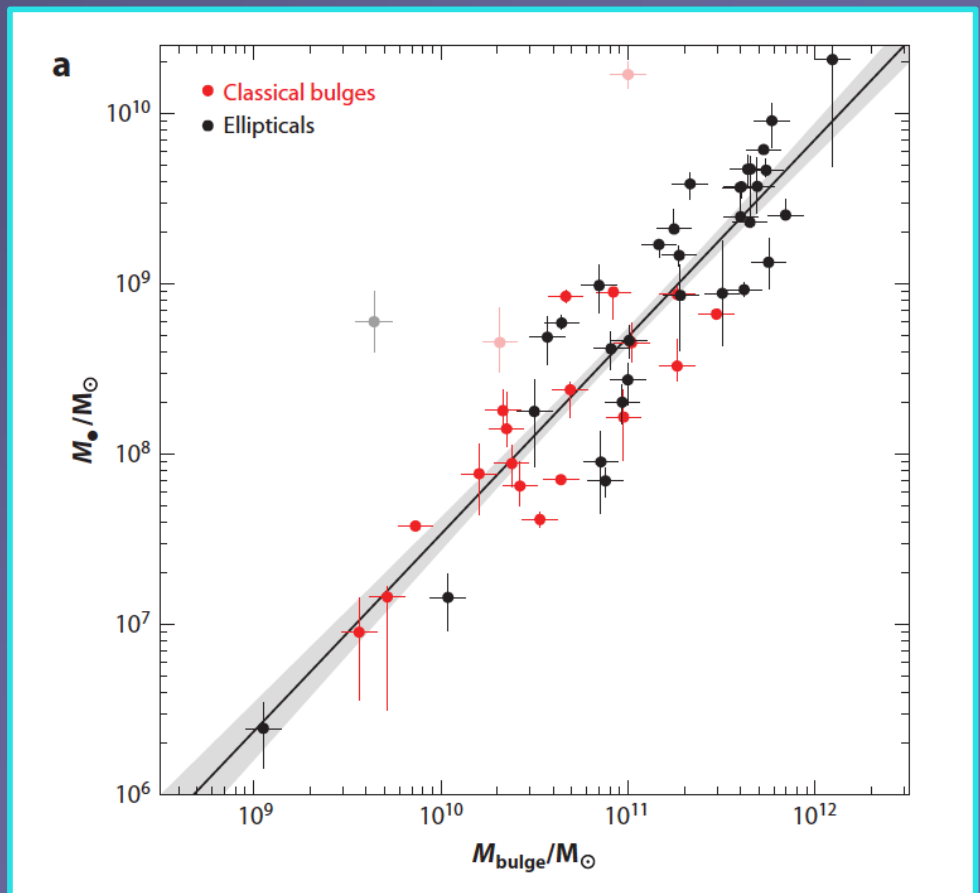
Early massive seed BHs:

$$M_{\text{bh}}/M_* \sim \infty$$

stay outliers for few 100 Myr

when $M_{\text{bh}} \sim 10^7 M_{\odot}$ and

$$M_{\text{bh}}/M_* > 1$$



Kormendy & Ho (2013)

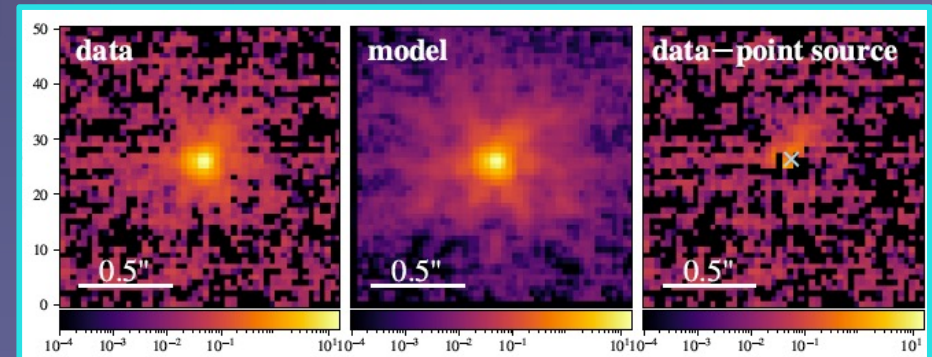
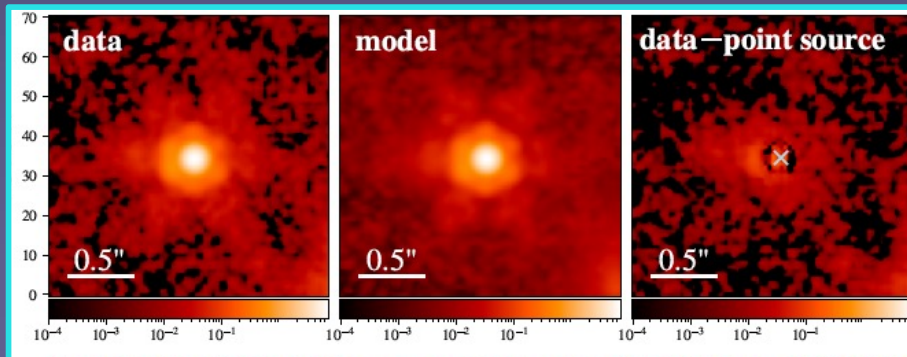
BH mass to host galaxy mass ratio

Ding et al. 2023; arxiv:2211.14329, Nature (submitted)

Extended starlight from host galaxies detected for the first time
JWST images for two $z \sim 6.4$ quasars

J2255+0251 $z=6.34$

J2236+0032 $z=6.40$



$$M_* = 3.4 \times 10^{10} M_\odot$$

$$M_* = 9.1 \times 10^{10} M_\odot$$

$$M_{\text{bh}} \sim 1.2 \times 10^9 M_\odot$$

$$M_{\text{bh}} \sim 1.9 \times 10^8 M_\odot$$

$$\rightarrow M_{\text{bh}}/M_* \sim 0.035$$

$$\rightarrow M_{\text{bh}}/M_* \sim 0.02$$

Conclusions

- **H₂ molecules control early massive black hole formation.** Chemically pristine primordial gas falls into protogalaxies at accretion rates $100-10^5$ times higher than in present-day
- Yields massive $10^6 M_{\odot}$ BHs via **supermassive star** or **hyper-accretion** onto stellar-remnant BH within first few 100 Myr
- In **ultra-dense star clusters**, and/or with the help of **gas disk torques**, black holes can also merge efficiently
- Combination of **gravitational waves** (probing mergers) and **optical/X-ray telescopes** (probing accretion) offer diagnostics of early black hole assembly

Thanks!